

# Analisi Matematica 1

## Canale D

10 novembre 2011

### ESERCIZIO 1

Calcolare i seguenti limiti

$$1. \lim_{x \rightarrow 0^+} \frac{x^2 - \sin^2 x}{x^3(e^x - \cos x)}$$

$$2. \lim_{x \rightarrow 0^+} \frac{x^5[(e^{x^3})^2 - 1]}{(1 + x^8)^{\frac{1}{2}} - (1 + x^8)^{\frac{1}{3}}}$$

$$3. \lim_{x \rightarrow 0^+} \frac{\tan x - x}{(1 - \cos x) \sin x}$$

$$4. \lim_{x \rightarrow 0^+} \frac{x \arcsin x - x^2}{(1 + x^4)^{\frac{1}{2}} - \cos x^2}$$

$$5. \lim_{x \rightarrow 0^+} \frac{\sin x^3 - \sin^3 x}{x^3(\cos x^3 - \cos^3 x)}$$

$$6. \lim_{x \rightarrow 0^+} \frac{\sqrt{1-x} - \cos \sqrt{x}}{\ln[\ln(e+x^2)]}$$

$$7. \lim_{x \rightarrow 0^+} \frac{\sinh x - \sin x}{x^3}$$

$$8. \lim_{x \rightarrow 0^+} \frac{(1+x)^{\frac{1}{x}} - e}{x}$$

$$9. \lim_{x \rightarrow 0^+} \frac{\sin^2 x - \sin x^2}{x^2 \ln(\cos x)}$$

$$10. \lim_{x \rightarrow 0^+} \frac{1 - e^{-x^2} + x^3 \sin(1/x)}{x^2}$$

## ESERCIZIO 2

Tracciare il grafico delle seguenti funzioni

$$1. f(x) = \sqrt{x+1} - \sqrt{x}$$

$$2. f(x) = -\ln(\sin x)$$

$$3. f(x) = (x^2 + 2x)e^x$$

$$4. f(x) = (x-2)e^{\frac{x}{x-1}}$$

$$5. f(x) = \frac{\ln x}{x^2}$$

$$6. f(x) = \cos x e^{\frac{1}{2} \sin x}$$

$$7. f(x) = 2x - \arcsin x$$

$$8. f(x) = \ln(1 + 2 \sin^2 x)$$

$$9. f(x) = \frac{x}{x+1} e^{-x}$$

$$10. f(x) = \frac{\arctan x}{x}$$